Image Analysis Tools
Biophysical Techniques Lecture Series 2020

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Outline

1. Image formation
2. Signal-to-noise enhancement
3. Deconvolution
4. Visualization & analysis
5. Access & training
Resolution criterion

- The image of a point through a circular aperture is an Airy function

\[ I(\theta) = \left( \frac{2 J_1(x)}{x} \right)^2 \]

with \( x = k a \sin \theta = kNAr \), \( k = \frac{2\pi}{\lambda} \), \( a \) the aperture radius.

- Rayleigh criterion: Two points are separables if the maximum corresponds to the first minima of the other spot \( (x \approx 3.83) \):

\[ \Delta_{xy} = \frac{0.61\lambda}{NA} \]

Ex: \( NA = 1.42 \), \( \lambda = 520nm \), \( \Delta = 208.68nm \)
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Optical sectioning

- Slice in 3D by defocusing the sample
- Depth of field of the microscope:
  \[ \Delta z \approx \frac{\lambda n}{NA^2} \]
  with \( n \) the index of the medium between the coverslip and the objective
- Many techniques exist to achieve optical sectioning (Confocal, TIRF, Structured Illumination)

Fig. 2: Depth of field in photography
Fig. 3: Depth of field vs numerical aperture
Point Spread Function

Definition

- Image of a point source
- Impulse response of the optical system

Properties

- Characterize the aberation of the microscope
- The image of an object is the convolution of this object by the point spread function of the microscope
Gibson and Lanni theoretical model

- By computing the difference of optical path:

\[ h(r, z) = \left| \frac{C}{d} \int_0^1 J_0 \left( \frac{ka\rho}{z} \right) e^{i\delta(\rho)} \rho \, d\rho \right|^2 \]

with \( k \) wave vector \((2\pi/\lambda)\), \( \delta(\rho) \) the optical path difference, 
\[ a = dNA/\sqrt{M^2 - NA^2}, \] NA the numerical aperture and \( M \) the magnification.

- Need to know all the parameters of the system

- May be able to adapt the model within the sample (spherical aberrations)
Experimental measure

- A measure of the impulse response can be obtained by acquiring the image of an object smaller than the resolution.
- We can use fluorescent beads or gold particle mounted in a medium similar to the one used to image the sample.

![Fig. 4: Axial and lateral view of a fluorescent bead (100nm) using a widefield microscope.](image)

- **Drawbacks**
  - Noisy measures
  - Need to have exactly the same condition than the sample (pixel size, binning, wavelength, mounting medium,...)
- **Advantage:**
  - Can capture complex aberrations due to the imperfection of the objective (but better hope the objective is in good state.)
Linear shift invariant system

- The output of a **linear shift invariant** system is the convolution of the input by the impulse response of the system.

\[ \text{Input} \rightarrow \text{System} \rightarrow \text{Output} \]

Fig. 5: Linear shift invariant system

- If we approximate the microscope as a LSI, then the acquired image is the **convolution** of the PSF and the sample.

\[ \text{Sample} \rightarrow \text{Microscope} \rightarrow \text{Image} \]

Fig. 6: Linear shift invariance approximation

- Counter example: spherical aberrations are function of depth
Linear shift invariant system

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  **Input** $\rightarrow$ **System** $\rightarrow$ **Output**

  ![Fig. 5: Linear shift invariant system](image)

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  ![Sample $\rightarrow$ PSF $\rightarrow$ Image](image)

  ![Fig. 6: Linear shift invariance approximation](image)

- Counter example: spherical aberrations are function of depth
Convolution

- **Linear combination** of intensity values for neighbours

\[ I[n] = a \cdot I[n - 1] + b \cdot I[n] + c \cdot I[n + 1] \]

- Coefficients \([a, b, c]\) define an array \(h\) called **filter**:


- We often denote \(h \ast l\) the convolution of \(l\) by \(h\).
1D Example

Convolutions of two rectangular functions

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The image shows two rectangular functions graphed against each other. The x-axis ranges from -3 to 3, and the y-axis ranges from 0 to 2. The red function is positioned from -2 to 0, while the blue function is from 0 to 1. The convolution of these two functions is visually represented by the area where they overlap, indicating the result of the convolution operation in the context of signal processing and mathematics.
1D Example

Convolutions of two rectangular functions
1D Example

Convolutions of two rectangular functions

![Graph showing convolutions of two rectangular functions]
1D Example

Convolutions of two rectangular functions

Graph showing the convolution of two rectangular functions.
1D Example

Convolutions of two rectangular functions

-3 -2 -1  1  2  3
-3 -2 -1  1  2  3

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1D Example

Convolutions of two rectangular functions
1D Example

Convolutions of two rectangular functions
Thick brush

- The convolution can be seen as a brush in use for painting
Decomposition in sine waves

- Square wave as sum of sine function:

\[ f(x) = \sum_{n=1}^{\infty} \frac{1}{n} \sin nx = 1 + \sin(x) + \frac{1}{3} \sin(3x) + \frac{1}{5} \sin(5x) + \cdots \]

![Signal and Spectrum Graph](image)

Fig. 8: Rectangle function decomposed into a series of sine functions.
Frequency domain

- Discrete Fourier Transform
  \[ \tilde{I}_k = \sum_{n=0}^{N-1} I_n \cdot (\cos(-2\pi kn/N) + i \sin(-2\pi kn/N)) \]

- The **Fast Fourier Transform** allows to speed-up the computation

- Spatial information “lost”

- Convolution \( \Leftrightarrow \) Multiplication

Fig. 9: Amplitude and phase of the Fourier transform of the top images.
**Optical transfer function**

**Definition**
The optical transfer function is the Fourier transform of the point spread function.

**Properties**
- Complexe values
- Contains the same information that the point spread function
- The modulus is called the modulation transfer function
- Its value vanishes beyond the cut-off frequency (resolution limit)

![Fig. 10: MTF in 2D computed as the autocorrelation of a disk.](image)
Widefield & Confocal PSF

Fig. 11: The three-dimensional point spread functions (a,c) and corresponding modulation transfer functions (b,d) of a wide-field microscope (a,b) and confocal microscope (c,d). In both cases the numerical aperture of the objective is 1.49 and the refractive index of the medium 1.52. The wavelength of the emitted light is assumed to be 600 nm and, in case of the confocal microscope, that of the excitation light 500 nm with circular polarization. The colors as shown on the logarithmic color bar indicate the irradiance (a,c) and spectral density (b,d) normalized to the maximum value. (cc) Tom.vettenburg at English Wikipedia
Spherical aberrations

- The rays on the edge of the lens do not intersect at the same point than the ones coming from the center.
- Microscope objectives are corrected for spherical aberrations
- In practice spherical aberration comes from
  - index mismatch (use the right lens: oil/water/air)
  - coverslip thickness (objectives are optimized for 0.17mm coverslip)
  - depth (across the z-stack, the PSF is varying due to the intermediate layers of different refractive index)

Fig. 12: Origin of spherical aberration.

Fig. 13: Cover glass thickness vs half-width intensity distribution. © http://www.olympusmicro.com
Spherical aberrations

- Characterized by an asymmetry in axial (Z) direction

Fig. 14: Longitudinal sections through a focused beam with negative (top row), zero (middle row), and positive spherical aberration (bottom row). The lens is to the bottom.
Chromatic aberrations

- The refractive index of materials depends on the wavelength $\lambda$
- The focus point of the lens depends on $\lambda$
- High quality objective are corrected for achromatism by combining doublet of lens (flint/crown)
- A change of dichroic filter might affect the lateral position of the focal point
Noise sources

Definition [signal processing]
In signal processing, noise is defined as un-wanted signal...

- Out of focus light, autofluorescence, dark current, shot noise, hot pixels?

Definition [statistic]
Noise is the variation of signal obtained by repeating the measurement.

- **shot noise**: the counting process lead to a Poisson distribution for the number of generated photo-electrons.
- **dark current**: even in the total obscurity, photo-electron are created and generate a tiny current
- **read-out**: errors made when measuring the voltage at each pixel
Random measurements

Measurements probability

true value

measure

SNR

SNR \sim \frac{N}{\sqrt{N}} = \sqrt{N}

Signal to noise ratio (SNR)

Number of photons

Number of photons

Short exposure (10ms)

Long exposure 1.5s

Probability

0

0.1

0

2

4

6

8

10

12

14

16

0

20

40

60

80

100

0

2

4

6

8

10

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Noise model & characterization

Assuming for each pixel $i$ of the image:

$$Y_i = g_0 N_i + \varepsilon_i$$

where

- $Y_i$ intensity
- $N_i \sim \mathcal{P}(\mu_i)$ photo-electron
- $\varepsilon_i \sim \mathcal{N}(m, \sigma_\varepsilon^2)$ thermal fluctuations

this leads to

$$\text{Var}[Y_i] = g_0 \mathbb{E}[Y_i] + \sigma_\varepsilon^2 - g_0 m$$

**Variance stabilization transform**

$$\mathcal{T}(Y_i) = \frac{2}{g_0} \sqrt{g_0 Y_i + \frac{3}{8} g_0^2 + e_{\text{DC}}} \sim \mathcal{N}(0,1)$$

![Fig. 17: Noise variance vs intensity empirically measured on a sCMOS camera.](image)
Background and uneven illumination

- Intensities are corrupted by a background and an non-uniform illumination profile.

- Non uniformity introduces
  - bias in intensity quantification
  - problem when tiling images.

- Background subtraction is not valid and make things worse in some case.
The microscope produces blurred and noisy images...
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Non-local image denoising

Non–Local Means principle

- Compare *patches* instead of pixels
- Average repeats in a large neighborhood
- Minimize the sum of the difference between patches

Iterative refinement

- Growing 4D neighborhood
- Statistical patch distance
- Bias-variance trade-off

Fig. 18: Patch exploration
Denoising benchmark
Using acquired images

F-actin/Tubulin/DNA

3.5s exposure time

50ms exposure time
Denoising benchmark
Using acquired images

3.5s exposure time

50ms exposure time denoising
Signal-to-noise improvement

Exposure time (ms)

PSNR (dB)

before

after

28 / 56
Signal-to-noise improvement

Exposure time (ms) vs. PSNR (dB)

- Red line: before
- Green line: after

20ms exposure time corresponds to a PSNR of approximately 28 dB before improvement and 56 dB after improvement.
Signal-to-noise improvement

Exposure time (ms)

PSNR (dB)

before

after

20ms

360ms

20

360

20 / 360

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Signal-to-noise improvement

![Graph showing signal-to-noise improvement with exposure time.](Image)

- PSNR (dB) before and after with exposure times from 20ms to 360ms.
- The graph shows a significant improvement in PSNR with an exposure time increase from 20ms to 360ms, indicated by a factor of 18x.
Fig. 19: Confocal image of developing Drosophila – Yara Sanchez-Corrales
Denoising from ImageJ/Fiji

- Integration as a macro
- Calling the native code
- Running locally

Fig. 20: Denoising interface and macro from Fiji
Batch processing on the cluster

1) copy the software on istore
2) copy the images on istore
3) launch the command

PC

Istore

hex

node #1

... 

node #3000
nd-safir software

n-dimensional spatially-adaptive filtering

- Process multi-dimensional data (5D)
- Parallel software rewritten (c++) at MRC-LMB
- Running on the cluster (single node) with helper scripts
- Bridge with ImageJ/Fiji

Integration in commercial solutions:
- OMEROC image management tool
- OMX
- Metamorph plugin (Roper Scientific SAS)
- Photometrics Prime Enhance sCMOS camera (FPGA)
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Fig. 21: Before (left) and after (right) deconvolution images. Experimental point spread functions were generated for the red, green, and blue channels on an epifluorescence microscope and then used to deconvolve a standard Invitrogen Fluocells #1 prepared slide, containing bovine pulmonary artery endothelial cells stained for mitochondria (red), F-actin (green), and nuclei (blue).
Why is it difficult?

- Convolution is equivalent to a multiplication by the OTF in Fourier space:
  \[ F = H \times U \]

- Can we deconvolve an image by dividing the image by the OTF?
  \[ U = \frac{F}{H} \]

- We saw that
  - The OTF vanishes beyond the resolution limit.
  - The noise kicks in even before this limit and would be amplified.

- Deconvolution is an “ill-posed” problem, we need to add constraints:
  - Positivity,
  - Smoothness (limit the number of iterations/add constraints).
Deconvolution algorithm

1. **Estimate of object**
2. **PSF**
3. **Measured image**
4. **Apply correction image**
5. **Compute correction image and the quality measure**
6. **Stop if sufficient quality is reached**
Huygens: step by step

1. Load the data (keep original format & metadata)
2. Edit the parameters
3. Inspect the data (hot pixels, saturation)
4. Define a PSF (theoretical vs measured)
5. Launch a deconvolution (several algorithm available)
6. Inspect the result (3D rendering, twin slicer)
7. Perform a chromatic correction
Main interface
Microscopy parameters

- Display the required informations related to the acquisition
- Indicate if these parameters are consistent
- Can be read in from metadata which accompany the RAW images.
- Keep the data in the original format
Algorithm selection and tuning
Twin slicer

- Synchronize views of 2 images
- Allows to inspect the image after deconvolution
Simulated Fluorescence Process

- Simulates how the object’s excited matter emits light forming a scene
- Based on ray tracing
Chromatic Aberration Corrector

- Register channels using
  - Cross correlation
  - Center of mass
- When performed after deconvolution, the higher SNR improves the registration
- Improves colocalization analysis
STED deconvolution

- Not only wide-field image can be deconvolved
- Huygens supports various imaging modality
  - Wide-field
  - Confocal
  - Light-sheet
  - STED
- Due to the non-linearity of the deconvolution process, extra resolution can be claimed.
- Here the lateral jitter correction, proved essential in improving the image quality.

Fig. 22: FWHM improvement toward 22nm ©Microscopy Today Nov 2013
DeconvolutionLab2 & PSF Generator

- Combine DeconvolutionLab2 and the PSF Generator plugin to deconvolve images
- Need to manually check background level

Fig. 23: PSF Generator from Fiji
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Bitplane Imaris

- Organize (group/conditions)
- Visualize (Volume rendering, isosurfaces)
- Analyze (spot detection, tracking, segmentation)
Organize

- All data are stored in an **Arena**
- Files can be grouped in an **assay** which can contain several **groups**.
Visualization

- A scene can be composed of several objects
  - Digital rendering
  - Surfaces
  - Spots (3D balls)
  - Tracks (3D filaments)
- A movie editors allows to create 3D animations easily
Image analysis

- Several analysis methods are available:
  - Spot detection and tracking
  - Segmentation
  - Neuron tracing
- You can then export extracted measurements
  - to Excel
  - via ImarisXT to make a bridge with Matlab
- Or use the statistical data plotting in Imaris.
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Image analysis softwares

- Analysis room located in room 1N120
- Softwares:
  - SVI Huygens (2)
  - Bitplane Imaris (3)
  - Nikon NIS Element General Analysis (1)
  - Offline version of
    - Leica LAS
    - Nilon NIS Element
    - Zeiss Zen
  - ImageJ/Fiji (6)
  - Mathworks Matlab (1)
  - R (1)

Fig. 26: Analysis room 1N120
Data management

• Acquisition stations
  • Temporary (regular clean up)
  • When disk are full the system slows down

• Temporary storage micro-nas-1
  • \sim 14\text{TB} NAS
  • \textbf{Shared} with all users
  • Temporary (regular clean up)
  • No mirroring (less secure)
  • RAID (support disk failure)
  • Good for exchanging data with us

• Long term archiving with istore
  • 500GB max
  • \textbf{secure} (mirrored outside the building)
  • accessible only by you
  • Good for keeping published raw data
Getting Help & Training

- **Subscribe** to the confocal list by sending an email to listmanager@mrc-lmb.cam.ac.uk with the text “subscribe confocal-list” in the message body.
- **Book a training** on an advanced imaging software
  - Huygens (Jon, Jérôme, Nick)
  - Imaris (Jon, , Jérôme, Nick)
  - Nikon NIS Element (Nick)
- **Attend a course**
  - Introduction to ImageJ macro programming (Jérôme)
  - Mastering Nikon NIS Element general analysis (Nick)
  - Introduction to image processing (Jérôme)
- **Come in and have a chat** (room 2S459)
  - We can help with your ImageJ macro (debug/custom script)
  - Create specific analysis procedure (ImageJ/Matlab/R/C++)
Online learning ressources

- **ImageJ**
  - http://fiji.sc
  - http://cmci.embl.de/documents/ijcourses
  - https://github.com/jboulanger/introduction-to-imagej-macros/releases/tag/1.0.0

- **SVI Huygens** https://svi.nl
  - register to the wiki
  - get in touch directly with SVI team (TCL scripting)

- **Bitplane Imaris** http://www.bitplane.com/learning
  - Step-by-step tutorials
  - Webinars
  - Case studies
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